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06ES36

Third Semester B.E. Degree Examination, June/July 2014
Field Theory

Time: 3 hrs.

Max. Marks: 100

**Note: Answer any FIVE full questions, selecting
at least TWO questions from each part.**

PART – A

1.
 - a. Define 'electric field intensity' and derive the expression for field due to an infinite line of charge. (12 Marks)
 - b. Sheet of charge with $\rho_s = -40 \mu\text{C}/\text{m}^2$ located at $z = -0.5\text{m}$, line of charge with $\rho_l = -6\mu\text{C}/\text{m}$ line along y-axis, what is the net flux crosses the surface of a cube of 2m on an edge of centered at origin. (04 Marks)
 - c. Calculate \vec{D} in rectangular co-ordinates at $P(2, -3, 6)$ produced by a point charge $Q = 55\text{mC}$ located at $(-2, 3, 6)$. (04 Marks)

2.
 - a. Show that \vec{E} is a negative potential gradient of the potential V . (05 Marks)
 - b. Given potential field $V = 2x^2y - 5z$ and at a point $P(-4, 3, 6)$, obtain
i) V , ii) \vec{E} , iii) Direction of \vec{E} . (05 Marks)
 - c. Find the capacitance of coaxial cable of inner radius 'a' and outer radius 'b'. (05 Marks)
 - d. A special capacitor of 54pF of two concentric sphere differing in radii 4cm with air as dielectric medium, find their radii and also find energy stored in the capacitor for $V = 100\text{V}$. (05 Marks)

3.
 - a. Derive Poisson's and Laplace's equations and write Laplace's equation in cylindrical and polar coordinates. (06 Marks)
 - b. Determine whether the following potential fields satisfies Laplace's equation or not:
i) $V = x^2 + y^2 + z^2$; ii) $V = \rho \cos\phi + z$. (06 Marks)
 - c. Using Laplace's equation, find capacitance of metallic parallel plates. (08 Marks)

4.
 - a. Derive an expression for H at a point in the axis of solenoid. (06 Marks)
 - b. A circuit carrying current 5A, from rectangular hexagon inscribed in a circle of radius 1m, calculate B at the centre of hexagon. (04 Marks)
 - c. Show that $\int_s \vec{H} \cdot d\vec{l} = \int_s \nabla \times \vec{H} \cdot d\vec{S} = I$, with definition of the same. (10 Marks)

PART – B

5.
 - a. Obtain the expression for magnetic force on moving point charge and magnetic force on differential current element. (10 Marks)
 - b. Obtain the expression for inductance of coaxial cable. (06 Marks)
 - c. Calculate the inductance of solenoid of 200 turns, wound tightly on a cylindrical tube of 6cm dia, length of cable (solenoid) is 60cm in air for $\mu = 3 \times 10^{-2}\text{m}$. (04 Marks)

- 6 a. Explain Faraday's law and Lenz's law. (06 Marks)
 b. Write Maxwell's equations in differential form and integral form. (08 Marks)
 c. A circular cross section conductor of radius 1.5mm carries a current $i = 5.5\sin(4 \times 10^{10}t)\mu\text{A}$.
 Find amplitude of the displacement current density if $\sigma = 35\text{U/m}$, $\epsilon_r = 10$. (06 Marks)
- 7 a. Derive an equation for wave propagation in free-space. (10 Marks)
 b. State and prove Poyntings theorem. (06 Marks)
 c. A plane wave traveling in positive x-direction in a lossless unbounded medium having permeability 4.5 times that of free space and a permittivity twice that of the wave,
 i) Find phase velocity of the wave.
 ii) If E has only y-component with a amplitude 20 V/m, find the amplitude and direction of H. (04 Marks)
- 8 a. Derive the expression for transmission coefficient and reflection coefficient. (08 Marks)
 b. Show that $\text{SWR} = \frac{1+\Gamma}{1-\Gamma}$. (06 Marks)
 c. Given, $\Gamma = 0.5$, $\eta_1 = 300\Omega$, $\eta_2 = 300\Omega$, $E_{xi} = 100 \text{ v/m}$. Calculate incident, reflected and transmitted waves also find average power is conserved. (06 Marks)

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